



Mathematics Fundamentals Year 12 – Pure Mathematics

Knowledge	Skills
<b>Algebra and Functions</b>	
<ul style="list-style-type: none"><li>• Understand and use the laws of indices for all rational exponents</li><li>• Work with quadratic functions and their graphs</li><li>• The discriminant of a quadratic function, including the conditions for real and repeated roots</li><li>• Completing the square</li><li>• Solution of quadratic equations, including solving quadratic equations in a function of the unknown</li><li>• Express solutions through correct use of 'and' and 'or', or through set notation</li><li>• Represent linear and quadratic inequalities such as <math>y &gt; x + 1</math> and <math>y &gt; ax^2 + bx + c</math> graphically</li><li>• Understand and use graphs of functions; sketch curves defined by simple equations including polynomials, <math>y = \frac{a}{x}</math> and <math>y = \frac{a}{x^2}</math> (including their vertical and horizontal asymptotes)</li><li>• Interpret algebraic solution of equations graphically; use intersection points of graphs to solve equations</li><li>• Understand the effect of simple transformations on the graph of <math>y = f(x)</math> including sketching associated graphs:</li><li>• <math>y = af(x)</math>, <math>y = f(x) + a</math>, <math>y = f(x + a)</math>, <math>y = f(ax)</math></li></ul>	<ul style="list-style-type: none"><li>• Use and manipulate surds, including rationalising the denominator</li><li>• Solve simultaneous equations in two variables by elimination and by substitution, including one linear and one quadratic equation</li><li>• Solve linear and quadratic inequalities in a single variable and interpret such inequalities graphically, including inequalities with brackets and fractions</li><li>• Manipulate polynomials algebraically, including expanding brackets, collecting like terms and factorisation and simple algebraic division; use of the factor theorem</li></ul>



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Knowledge	Skills
<b>Coordinate Geometry in the (x,y) Plane</b>	
<ul style="list-style-type: none"><li>• Understand and use proportional relationships and their graphs</li><li>• Understand and use the equation of a straight line, including the forms <math>y - y_1 = m(x - x_1)</math> and <math>ax + by + c = 0</math></li><li>• Gradient conditions for two straight lines to be parallel or perpendicular</li><li>• Understand and use the coordinate geometry of the circle including using the equation of a circle in the form <math>(x - a)^2 + (y - b)^2 = r^2</math></li><li>• Use of the following properties:<ul style="list-style-type: none"><li>• the angle in a semicircle is a right angle</li><li>• the perpendicular from the centre to a chord bisects the chord</li><li>• the radius of a circle at a given point on its circumference is perpendicular to the tangent to the circle at that point</li></ul></li></ul>	<ul style="list-style-type: none"><li>• Be able to use straight line models in a variety of contexts</li><li>• Completing the square to find the centre and radius of a circle</li></ul>

Knowledge	Skills
<b>Further Algebra</b>	
<ul style="list-style-type: none"><li>• Understand and use the structure of mathematical proof, proceeding from given assumptions through a series of logical steps to a conclusion; use methods of proof, including: proof by deduction, proof by exhaustion, disproof by counter-example</li><li>• Understand and use the binomial expansion of <math>(a + bx)^n</math> for positive integer <math>n</math>; the notations <math>n!</math> and <math>{}_nC_r</math>; link to binomial probabilities</li></ul>	<ul style="list-style-type: none"><li>• Manipulate polynomials algebraically, including expanding brackets and collecting like terms, factorisation and simple algebraic division; use of the factor theorem</li></ul>



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Knowledge	Skills
<b>Trigonometry</b>	
<ul style="list-style-type: none"><li>• Understand and use the definitions of sine, cosine and tangent for all arguments; the sine and cosine rules; the area of a triangle in the form <math>\frac{1}{2}ab \sin C</math></li><li>• Understand and use the sine, cosine and tangent functions; their graphs, symmetries and periodicity</li><li>• Understand and use <math>\tan \theta = \frac{\sin \theta}{\cos \theta}</math></li><li>• Understand and use <math>\sin^2 \theta + \cos^2 \theta = 1</math></li></ul>	<ul style="list-style-type: none"><li>• Solve simple trigonometric equations in a given interval, including quadratic equations in sin, cos and tan and equations involving multiples of the unknown angle</li></ul>

Knowledge	Skills
<b>Vectors (2D)</b>	
<ul style="list-style-type: none"><li>• Use vectors in two dimensions</li><li>• Understand and use position vectors; calculate the distance between two points represented by position vectors</li><li>• Use vectors to solve problems in pure mathematics and in context, (including forces)</li></ul>	<ul style="list-style-type: none"><li>• Calculate the magnitude and direction of a vector and convert between component form and magnitude/direction form</li><li>• Add vectors diagrammatically and perform the algebraic operations of vector addition and multiplication by scalars, and understand their geometrical interpretations</li></ul>



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Knowledge	Skills
<b>Differentiation</b>	
<ul style="list-style-type: none"><li>Understand and use the derivative of <math>f(x)</math> as the gradient of the tangent to the graph of <math>y = f(x)</math> at a general point <math>(x, y)</math>; the gradient of the tangent as a limit; interpretation as a rate of change</li><li>Second derivatives</li><li>Identify where functions are increasing or decreasing</li></ul>	<ul style="list-style-type: none"><li>Sketching the gradient function for a given curve</li><li>Differentiation from first principles for small positive integer powers of <math>x</math></li><li>Differentiate <math>x^n</math>, for rational values of <math>n</math>, and related constant multiples, sums and differences</li><li>Apply differentiation to find gradients, tangents and normals, maxima and minima and stationary points</li></ul>

Knowledge	Skills
<b>Integration</b>	
<ul style="list-style-type: none"><li>Know and use the Fundamental Theorem of Calculus</li></ul>	<ul style="list-style-type: none"><li>Integrate <math>x^n</math> (excluding <math>n = -1</math>), and related sums, differences and constant multiples</li><li>Evaluate definite integrals; use a definite integral to find the area under a curve</li></ul>

Knowledge	Skills
<b>Exponentials and Logarithms</b>	
<ul style="list-style-type: none"><li>Know and use the function <math>a^x</math> and its graph, where <math>a</math> is positive</li><li>Know and use the function <math>e^x</math> and its graph</li></ul>	<ul style="list-style-type: none"><li>Solve equations of the form <math>a^x = b</math></li><li>Use logarithmic graphs to estimate parameters in relationships of the form <math>y = ax^n</math> and <math>y = kb^x</math>, given data for <math>x</math> and <math>y</math></li></ul>



## Mathematics Fundamentals Year 12 – Pure Mathematics

- Know that the gradient of  $e^{kx}$  is equal to  $ke^{kx}$  and hence understand why the exponential model is suitable in many applications
- Know and use the definition of  $\log_a x$  as the inverse of  $a^x$ , where  $a$  is positive and  $x \geq 0$
- Know and use the function  $\ln x$  and its graph
- Know and use  $\ln x$  as the inverse function of  $e^x$
- Understand and use the laws of logarithms:

$$\log_a x + \log_a y = \log_a(xy)$$

$$\log_a x - \log_a y = \log_a\left(\frac{x}{y}\right)$$

$$k\log_a x = \log_a x^k \quad (\text{including, for example, } k = -1 \text{ and } = -\frac{1}{2})$$

- Understand and use exponential growth and decay; use in modelling (examples may include the use of  $e$  in continuous compound interest, radioactive decay, drug concentration decay, exponential growth as a model for population growth); consideration of limitations and refinements of exponential models